Positional Notation

Also called place-value notation
- Each place represents a power of the base
- Each numeral is multiplied by positional value

E.g., base 10 (decimal):
\[(4273)_{10} = 3 \times 10^3 + 7 \times 10^1 + 2 \times 10^2 + 4 \times 10^1\]

Other Bases

Computer scientists tend to think in powers of 2:
- Hexadecimal (base-16) – use digits 0-9, a-f (or A-F)
  \[(4273)_{10} = (10b1)_{16} = 1 \times 16^3 + 11 \times 16^1 + 1 \times 16^0\]
- Octal (base-8) – mostly out of use now
  \[(4273)_{10} = (10261)_{8} = 1 \times 8^3 + 6 \times 8^1 + 2 \times 8^2 + 1 \times 8^1\]
- Binary! (0s and 1s)
  \[(4273)_{10} = (0001 0000 1011 0001)_2\]

Bits and Bytes

Computers work with bits – 0’s and 1’s
- (Positive) integers are represented in base 2:
  \[0_2 = 0, \quad 1_2 = 1, \quad 2_2 = 10, \quad 3_2 = 11, \quad 4_2 = 100, \quad 5_2 = 101, \text{ etc.}\]
- Computers organize bits into bytes – 8-bit chunks
- C++ data types are organized into bytes
  - char uses 1 byte
  - int uses 4 bytes
  - double uses 8 bytes
- Get size of a variable/object type with sizeof:
  \[\text{int sz_of dbl} = \text{sizeof(double)};\]
MEMORY

Computer memory is organized as an indexed array of bytes:

Addresses (traditionally given in hexadecimal)

It is traditional to represent memory as a vertical array.
All right thinking people start at the bottom and count up.

We say that the byte value 72 is stored at address 0x1004...

However, from the programmer's perspective, the value stored at 0x1004 depends on the type. It could be an int value (4 bytes)...

Or the start of a string...

Reference (address of) Operator &

Suppose this int value corresponds to the variable x:

```cpp
  int x = 1819043144;
```

We can obtain the address of x using the operator &:

```cpp
  cout << &x << endl; // prints 0x1004
```  
(Try it!)

Pointers

A pointer is a variable that stores an address:

```cpp
  int x = 1819043144;
  int* p = &x; // p now stores 0x1004
```

The type of the variable p is int*.

Note that int* is only for pointers to int; every type T has a corresponding pointer type T*.

You can write:

```cpp
  int* p;
  int* q = p; // compiler interprets them all the same.
```
**Dereference Operator ***

You usually don’t want to see the address itself, but what is at the address — you can get the pointed-to value by using *:

```cpp
int x = 1819043144;
int* p = &x;
cout << *p << endl;
```

The previous line outputs the same thing as:

```cpp
cout << x << endl;
```

**So Where Do Pointers Live…?**

In memory, of course!

```cpp
int x = 1819043144;
int* p = &x;
And yes, you can declare pointers to:
int* pp = &p;
int*** q = &pp;

p
x changed; p didn’t.
```

**Pointer Independence**

Suppose we change the value of x:

```cpp
int x = 1819043144;
int* p = &x;
x = 6;
```

We can also assign through the * operator:

```cpp
*p = 17;
```

**Assigning Through * **

Suppose we change the value of x:

```cpp
int x = 1819043144;
int* p = &x;
```

We can also assign through the * operator:

```cpp
*p = 17;
```

**Pointers As Variables**

Pointers can be assigned like any other variable:

```cpp
int x, y;
int* p = &x; // p points to x
int* q = p; // now q and p points to x
p = &y; // now p points to y, q to x
q = 15; // x now stores 15
```
The nullptr Pointer

- C++ defines a special keyword for pointers which do not currently point to anything: `nullptr`
  ```cpp
  int* p = nullptr;
  ```
- A null pointer is never a valid memory address:
  ```cpp
  int* p = nullptr;
  cout << *p << endl;  // crash
  *p = 42;  // also crash
  ```
- Prior to C++ 11, the value NULL was used instead of nullptr. You will see a lot of code using NULL.

POINTER NOTES

Dereferencing Pointers

- Given a pointer `p` to some value:
  ```cpp
  *p dereferences `p`, is equivalent to the value.
  ```
- Suppose `p` points to an object or structure:
  ```cpp
  (*p).foo dereferences `p` and accesses the member `foo`
  ```
- In the next lecture we'll see that array indexing is another kind of dereferencing:
  ```cpp
  p[i] == *(p + i)
  ```
  (But we'll have to explain pointer arithmetic first.)

Multiple Pointer Declaration

An oddity of C/C++: we must do
```cpp
int *p, *q;  // we have to use * for both even though int* is the type.
```
Otherwise:
```cpp
int *p, q;  // p is an int*, but q is an int
```

Up Next

- Today
  - Lab 1 due
  - Reading: Chapter 14.1-14.2
- Wednesday, January 16
  - Linked Lists
  - Reading: Chapter 14.4-14.6
- Friday, January 18
  - Lab 2 – I/O
  - APT 1 due
  - Project 1 assigned